Outline

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(September 3, 2007)

• Introduction

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 - ② Coordination and convention
 - ③ Testing mixed strategies
 - ④ Ultimatum game
- Experimental protocol

Recent branch of game theory using an *experimental approach*

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Empirical/descriptive analysis based on *data* (laboratory experiments) and *psychological facts*

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Why using such approach?

> Underline empirical regularities in human strategic behavior

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- > Characterize favorable/unfavorable conditions for the theory to work

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- > Evaluate new policies or institutions before implementing them in the field
- > Teaching tool of game theory and market mechanisms



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Advantages

- ① Highly controlled environment (\neq field studies)
- ② Easy to replicate



Figure 1: Daniel Kahneman (1934–) and Vernon L. Smith (1927-), Nobel Prize in Economics in 2002



"Beauty contest" and Depth of Reasoning

In "The General Theory of Employment, Interest, and Money", Keynes (1936) compares asset markets with beauty contests of some newspapers:

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In "The General Theory of Employment, Interest, and Money", Keynes (1936) compares asset markets with beauty contests of some newspapers:

"Professional investment may be likened to those newspaper competitions in which the competitors have to pick out the six prettiest faces from a hundred photographs, the prize being awarded to the competitor whose choice most nearly corresponds to the average preferences of the competitors as a whole; so that each competitor has to pick, not those faces which he himself finds prettiest, but those which he thinks likeliest to catch the fancy of the other competitors, all of whom are looking at the problem from the same point of view. It is not a case of choosing those which, to the best of one's judgment, are really the prettiest, nor even those which the average opinion genuinely thinks the prettiest. We have reached the third degree where we devote our intelligence to anticipating what the average opinion expects the average opinion to be . And there are some, I believe, who practice the fourth, fifth and higher degrees." (Keynes, 1936, Chapter 12).

Game Theory Moulin (1986): Simple game underlining such reasoning

Behavioral Game Theory

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- Announcing more than 70 is (weakly) dominated by 70
- With this reasoning, every player's announcement is in [0, 70], so 70% of the average is not larger than 49
- Announcing more than 49 becomes (weakly) dominated
- Announcing more than 35 becomes (weakly) dominated

- Announcing more than 70 is (weakly) dominated by 70
- With this reasoning, every player's announcement is in [0, 70], so 70% of the average is not larger than 49
- Announcing more than 49 becomes (weakly) dominated
- Announcing more than 35 becomes (weakly) dominated
- then 25, 18, ...

Iterated elimination of dominated strategies:

- Announcing more than 70 is (weakly) dominated by 70
- With this reasoning, every player's announcement is in [0, 70], so 70% of the average is not larger than 49
- Announcing more than 49 becomes (weakly) dominated
- Announcing more than 35 becomes (weakly) dominated
- then 25, 18, ...

which converges to 0

Iterated elimination of dominated strategies:

- Announcing more than 70 is (weakly) dominated by 70
- With this reasoning, every player's announcement is in [0, 70], so 70% of the average is not larger than 49
- Announcing more than 49 becomes (weakly) dominated
- Announcing more than 35 becomes (weakly) dominated
- then 25, 18, ...

which converges to 0

It is also easy to verify that announcing 0 is the unique Nash equilibrium

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Further readings: Camerer (2003, chap. 5), Nagel (1995) and Ho et al. (1998)

Coordination and Convention

Coordination and Convention

	Median choice													
	1	2	3	4	5	6	7	8	9	10	11	12	13	14
1	45	49	52	55	56	55	46	-59	-88	-105	-117	-127	-135	-142
2	48	53	58	62	65	66	61	-27	-52	-67	-77	-86	-92	-98
3	48	54	60	66	70	74	72	1	-20	-32	-41	-48	-53	-58
4	43	51	58	65	71	77	80	26	8	-2	-9	-14	-19	-22
5	35	44	52	60	69	77	83	46	32	25	19	15	12	10
6	23	33	42	52	62	72	82	62	53	47	43	41	39	38
7	7	18	28	40	51	64	78	75	69	66	64	63	62	62
8	-13	-1	11	23	37	51	69	83	81	80	80	80	81	82
9	-37	-24	-11	3	18	35	57	88	89	91	92	94	96	98
10	-65	-51	-37	-21	-4	15	40	89	94	98	101	104	107	110
11	-97	-82	-66	-49	-31	-9	20	85	94	100	105	110	114	119
12	-133	-117	-100	-82	-61	-37	-5	78	91	99	106	112	118	123
13	-173	-156	-137	-118	-96	-69	-33	67	83	94	103	110	117	123
14	-217	-198	-179	-158	-134	-105	-65	52	72	85	95	104	112	120

Behavioral Game Theory

Coordination and Convention

... Take your decision! ...

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10	-65	-51	-37	-21	-4	15	40	89	94	98	101	104	107	110
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Further readings: Camerer (2003, chap. 7)

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- \ldots + assumptions on attitude towards risk
- Biases of human perception of probabilities, and difficulty to make independent choices

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- A mixed strategy equilibrium can be seen as a population equilibrium where no single individual makes random choices
- Non-independent choices is consistent with an equilibrium in beliefs (Brandenburger, 1992; Aumann and Brandenburger, 1995)
- No assumption on risk attitude is required if there is only two possible payoffs in the game (cardinality of VNM utility functions)

Behavioral Game Theory

O'Neill (1987) Experiment
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					Nash	Empirical
	a	b	С	J	equilibrium	frequencies
a	-5	5	5	-5	0.20	0.221
b	5	-5	5	-5	0.20	0.215
С	5	5	-5	-5	0.20	0.203
J	-5	-5	-5	5	0.40	0.362
Nash equilibrium	0.20	0.20	0.20	0.40		
Empirical frequencies	0.226	0.179	0.169	0.426		

(105 rounds with 25 pairs of subjects)

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→ Aggregate behavior remarkably close to equilibrium predictions

Game Theory Camerer (2003, Figure 3.1, page 121) : General idea of the predictive power of mixed strategy Nash equilibrium in various experiments with a unique Nash equilibrium

Behavioral Game Theory

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 - If the offer is rejected the surplus is loss (0 for both)
- Last step of a more complicated negotiation problem





Backward Induction:



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The second player accepts every positive offer



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 \Rightarrow The first player keeps 10 euros (or 9.99 euros): $x \simeq 0$

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Remark. This explanation is NOT inconsistent with standard game theoretical models and expected utility theory





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Instructions.

- > Clear, detailed, and understandable for everyone
- > Read publicly (common knowledge)
- > In general, all information that is available to the game theorist should be made available to the subjects (\neq experiments in psychology)

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Matching and Reputation.

Repetition of the game should not interfere with the original rules of the game (supergame effects: reputation, threat, punishment) Game Theory

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Ordering Effect.

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Ordering Effect.

Several games can be implemented in the same experiment but all subjects should not play them in the same order because the order may significantly influence their behavior (learning, framing, ...)

Game Theory References

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